



# Charge and spin transport through Interference Single Electron Transistors

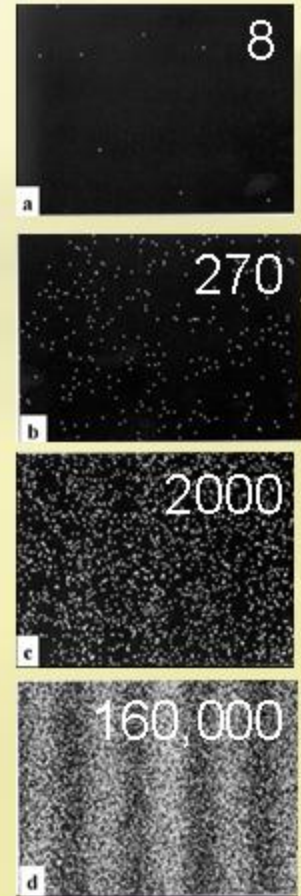
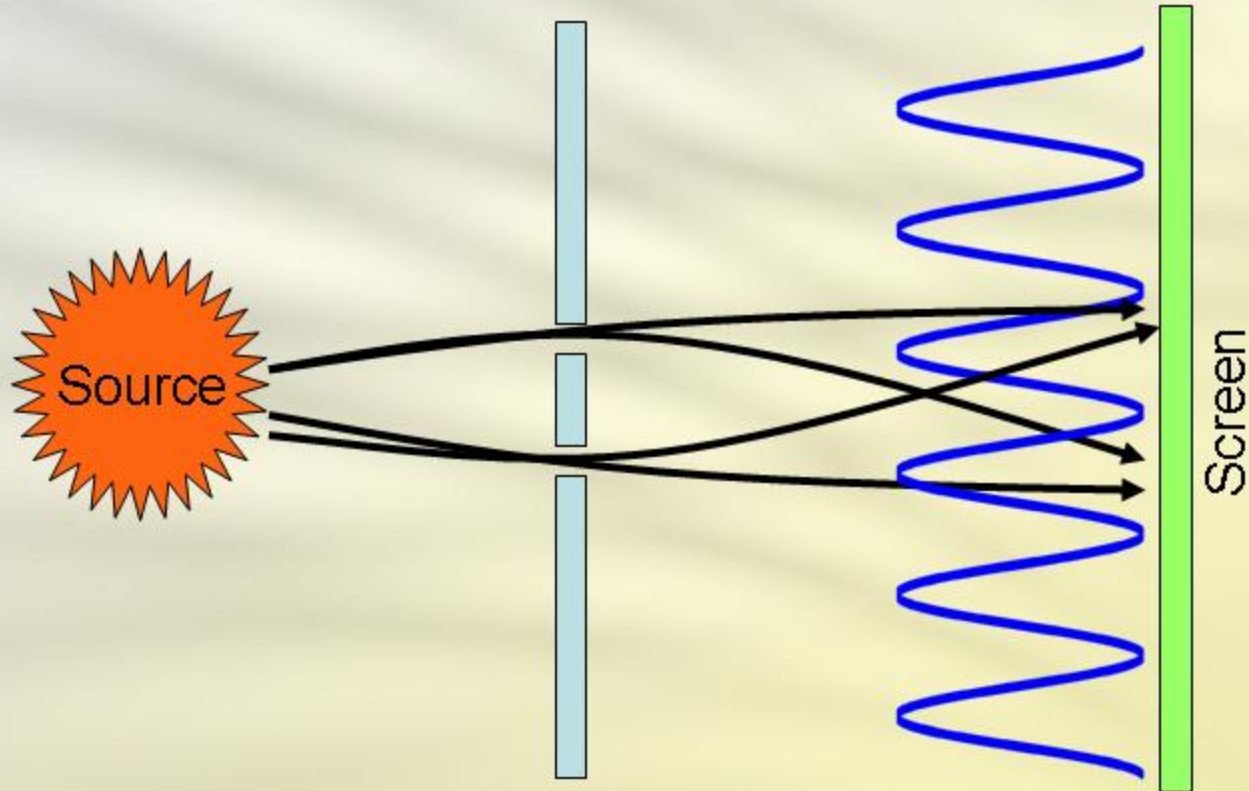
**Andrea Donarini**

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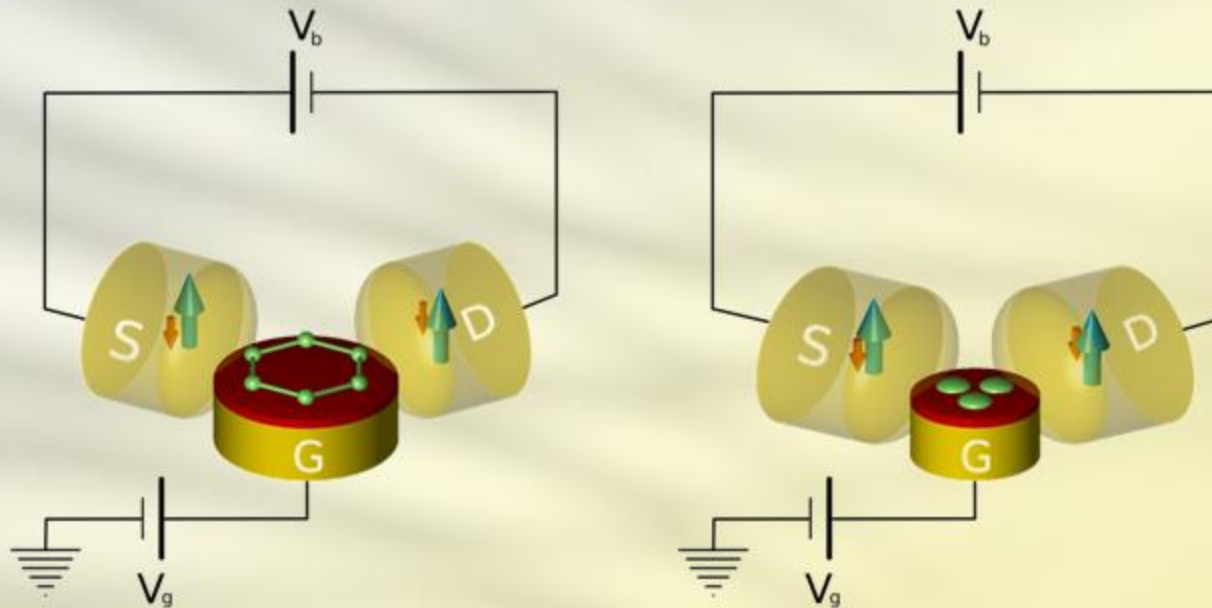
# Macroscopic interference

Young's light-interference experiment (1801)



Double-slit experiment with interference  
of single electrons (1961)

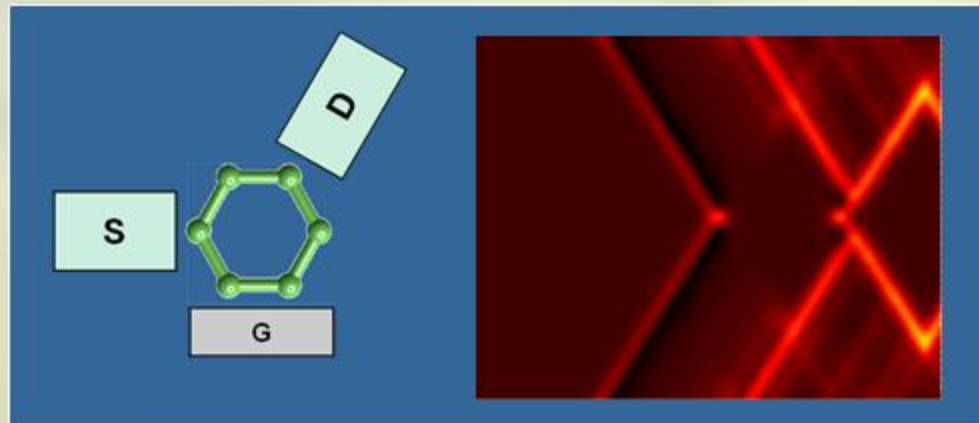
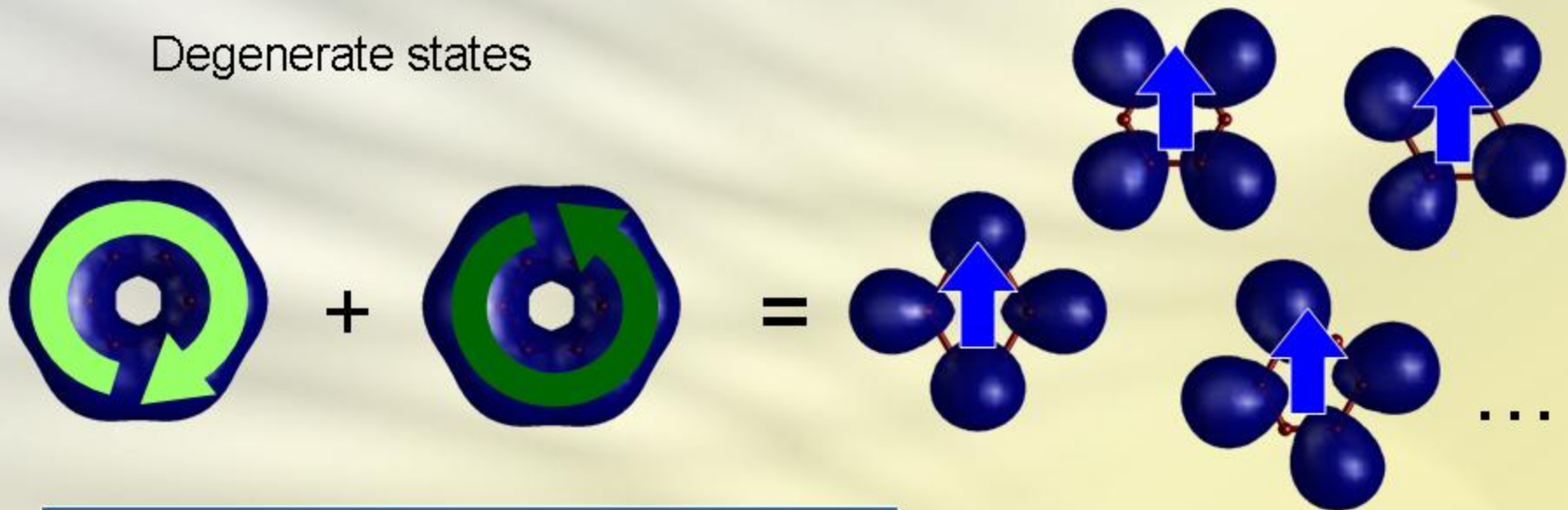
## ISET



The interference occurs between transmission paths involving  
orbitally (quasi-)degenerate states

# Intra-molecular interference

Degenerate states



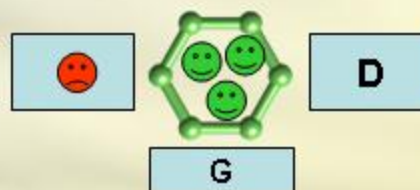
Interference visible in the **current** as a function of **bias** and **gate** voltages.

# (Benzene) ISET...

- **Weak coupling**
- **Coulomb** interaction
- Molecular **size**
- **Low** temperature



Coulomb  
blockade



$$\hbar\Gamma \ll k_B T \ll \Delta E_{\text{ex}}$$

- **Rotational** symmetry



Orbitally  
degenerate  
states

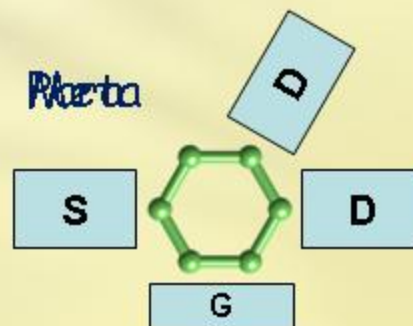


$$E_1 = E_2$$

- Contact **geometry**



Contact  
symmetry  
breaking



$$\frac{\gamma_{1L}}{\gamma_{2L}} \neq \frac{\gamma_{1R}}{\gamma_{2R}}$$

# ... with a magnetic flavour

- **Coulomb** interaction
- Molecular **size**



Exchange  
splitting

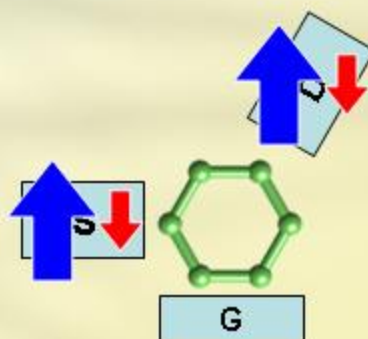


$$E_{\text{triplet}} \neq E_{\text{singlet}}$$

- Parallel  
**ferromagnetic**  
leads



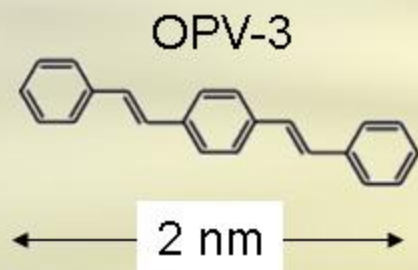
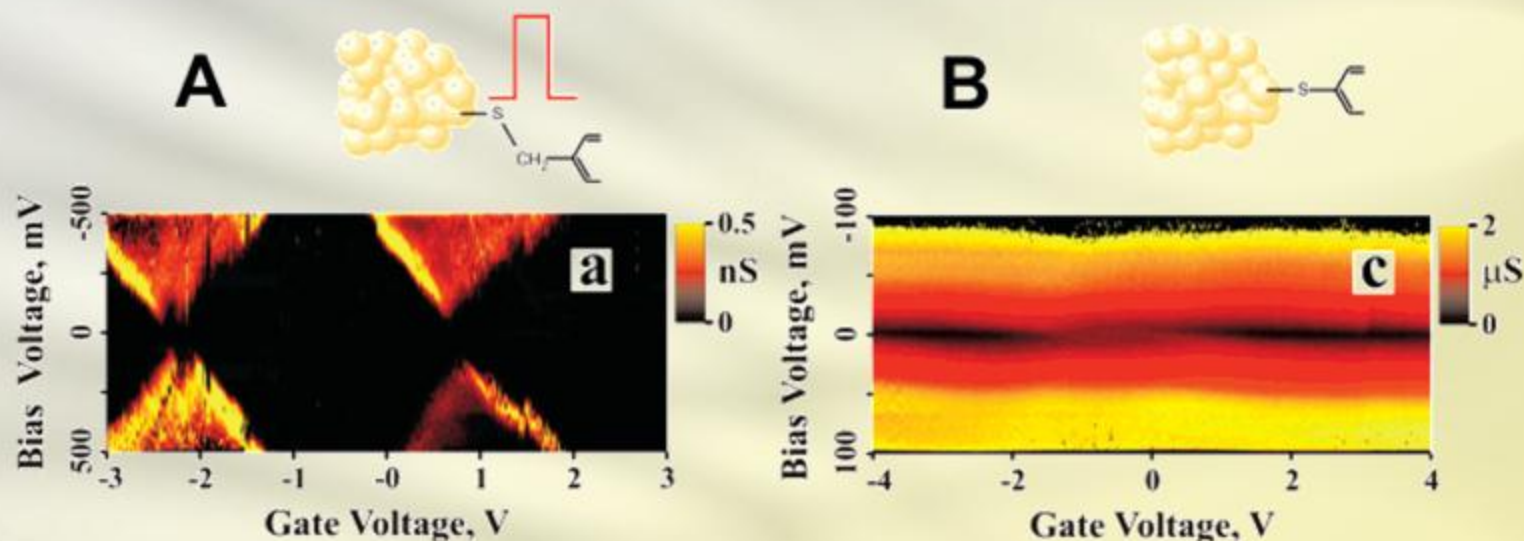
Spin  
symmetry  
breaking



$$\Gamma_{\alpha\uparrow} \neq \Gamma_{\alpha\downarrow}$$

The interplay between orbital and spin degree of freedom allows  
all-electrical spin control on the molecule.

# Coulomb blockade

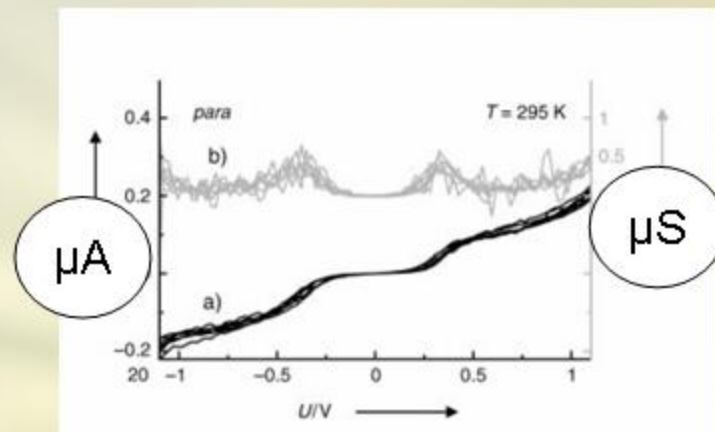
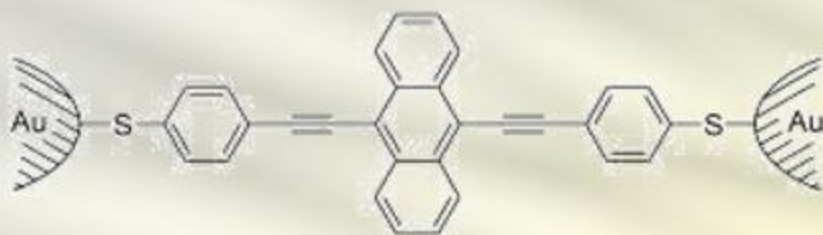


- **Gating** of 2 nm sized molecule
- **Weak coupling** realization with specific anchor groups

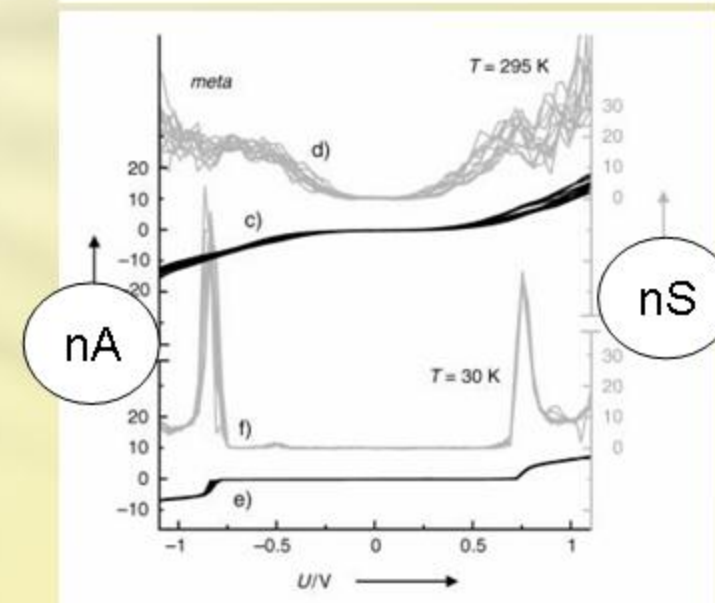
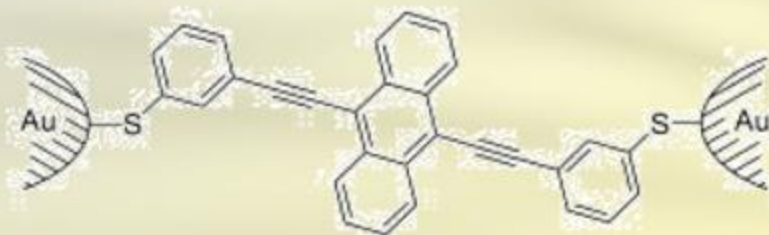
A. Danilov, S. Kubatkin, et al. Nanoletters **8**, 1 (2008)

# Symmetry breaking contacts

## Para configuration



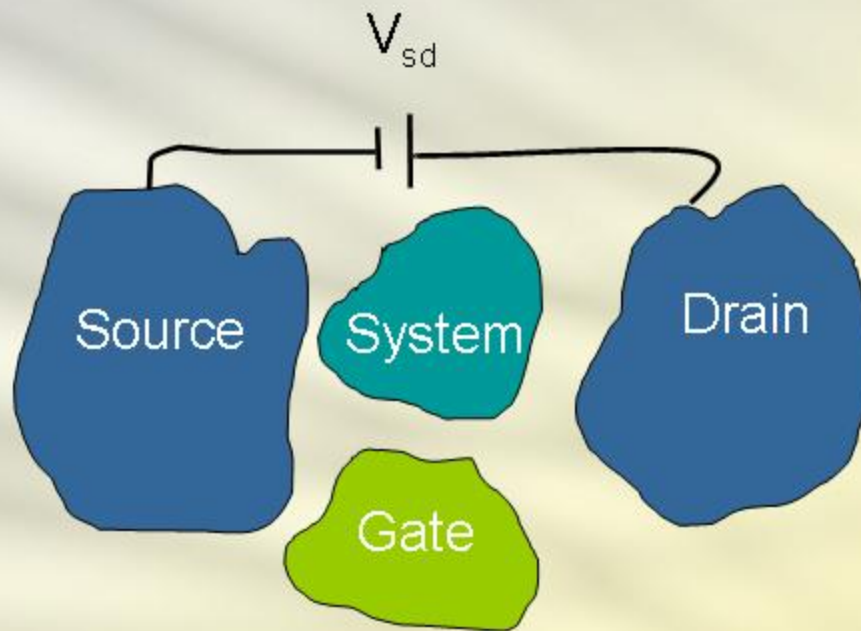
## Meta configuration



M. Mayor, H. Weber, et al. *Angew. Chem. Int. Ed.* **42** 5843 (2003)



# The Hamiltonian

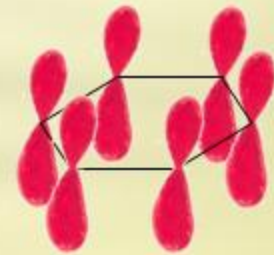


$$H = H_{\text{Sys}} + H_{\text{leads}} + H_{\text{tun}} \left\{ \begin{array}{l} H_{\text{Sys}} = H_{\text{ben}} / H_{\text{TD}} \\ H_{\text{leads}} = \sum_{\alpha k \sigma} (\epsilon_k - \mu_\alpha) c_{\alpha k \sigma}^\dagger c_{\alpha k \sigma} \\ H_{\text{tun}} = t \sum_{\alpha k \sigma} (d_{\alpha \sigma}^\dagger c_{\alpha k \sigma} + c_{\alpha k \sigma}^\dagger d_{\alpha \sigma}) \end{array} \right.$$

# Interacting isolated benzene

- The **Pariser-Parr-Pople** Hamiltonian for isolated benzene reads:

$$\begin{aligned}
 H_{\text{ben}}^0 = & \xi_0 \sum_{i\sigma} d_{i\sigma}^\dagger d_{i\sigma} + b \sum_{i\sigma} \left( d_{i\sigma}^\dagger d_{i+1\sigma} + d_{i+1\sigma}^\dagger d_{i\sigma} \right) \\
 & + U \sum_i \left( n_{i\uparrow} - \frac{1}{2} \right) \left( n_{i\downarrow} - \frac{1}{2} \right) \\
 & + V \sum_i \left( n_{i\uparrow} + n_{i\downarrow} - 1 \right) \left( n_{i+1\uparrow} + n_{i+1\downarrow} - 1 \right)
 \end{aligned}$$



- The **size** of the Fock space for the many-body system  **$4^6 = 4096$**  since for each site there are 4 possibilities:  $|0\rangle, |\uparrow\rangle, |\downarrow\rangle, |\uparrow\downarrow\rangle$
- Within this Fock space we diagonalize **exactly** the Hamiltonian.

# Symmetry of the ground states

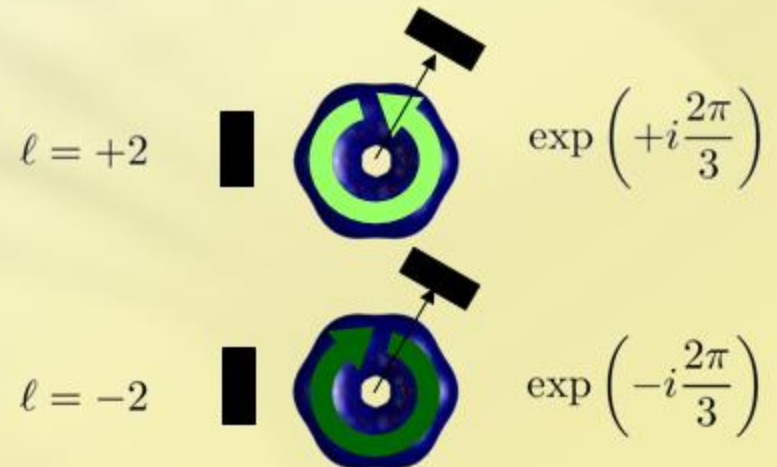
N	Degeneracy	GS energy[eV] (at $\xi = 0$ )	GS symmetry representation
0	1	0	$A_{1g}$
1	2	-22	$A_{2u}$
2	1	-42.25	$A_{1g}$
3	4	-57.42	$E_{1g}$
4	3	-68.875	$A_{2g}$
5	4	-76.675	$E_{1g}$
6	1	-81.725	$A_{1g}$
7	4	-76.675	$E_{2u}$
8	3	-68.875	$A_{2g}$
9	4	-57.42	$E_{2u}$
10	1	-42.25	$A_{1g}$
11	2	-22	$B_{2g}$
12	1	0	$A_{1g}$

## Rotation phase factors

Under rotation of an angle  $\phi = \frac{n\pi}{3}$

- $\mathcal{R}_\phi |6_g\rangle = |6_g\rangle$       No phase acquired

- $\mathcal{R}_\phi |7_g \ell\rangle = e^{-i\ell\phi} |7_g \ell\rangle$        $\ell = \pm 2$



# Generalized Master Equation

- We start with the **Liouville** equation:  $\dot{\rho} = -\frac{i}{\hbar}[\mathcal{H}, \rho]$



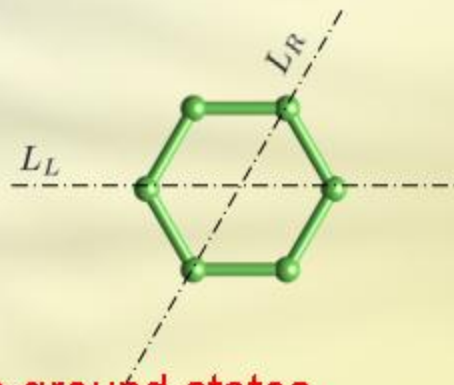
- We consider a reduced density matrix **block-diagonal** in spin, energy and particle number. We keep coherencies between **orbitally** degenerate states.
- The **Generalized Master Equation** is an equation of motion for the reduced density matrix. We calculate it in the lowest non-vanishing order in the coupling to the leads and in the Markov approximation. It reads:

$$\dot{\sigma} = \underbrace{-\frac{i}{\hbar}[H_{\text{sys}}, \sigma]}_{\text{Coherent dynamics}} - \underbrace{\frac{i}{\hbar}[H_{\text{eff}}, \sigma]}_{\text{Effective internal dynamics}} + \underbrace{\mathcal{L}_{\text{tun}}\sigma}_{\text{Tunnelling dynamics}}$$

# The effective Hamiltonian

The effective Hamiltonian is expressed in terms of **angular momentum** operators and **renormalization frequencies**:

$$H_{\text{eff}} = \sum_{\alpha\sigma} \omega_{\alpha\sigma} L_{\alpha}$$



In particular in the Hilbert space of the **7 particle ground states**

$$L_{\alpha} = \frac{\hbar}{2} \begin{pmatrix} 1 & e^{i2|\ell|\phi_{\alpha}} \\ e^{-i2|\ell|\phi_{\alpha}} & 1 \end{pmatrix}$$

$$\omega_{\alpha\sigma} = \frac{1}{\pi} \sum_{\sigma' \{E\}} \Gamma_{\alpha\sigma'}^0 \left[ \langle 7_g \ell \sigma | d_{M\sigma'} | 8\{E\} \rangle \langle 8\{E\} | d_{M\sigma'}^{\dagger} | 7_g m \sigma \rangle p_{\alpha}(E - E_{7_g}) + \langle 7_g \ell \sigma | d_{M\sigma'}^{\dagger} | 6\{E\} \rangle \langle 6\{E\} | d_{M\sigma'} | 7_g m \sigma \rangle p_{\alpha}(E_{7_g} - E) \right]$$

← Bias and gate dependent

# Current operator

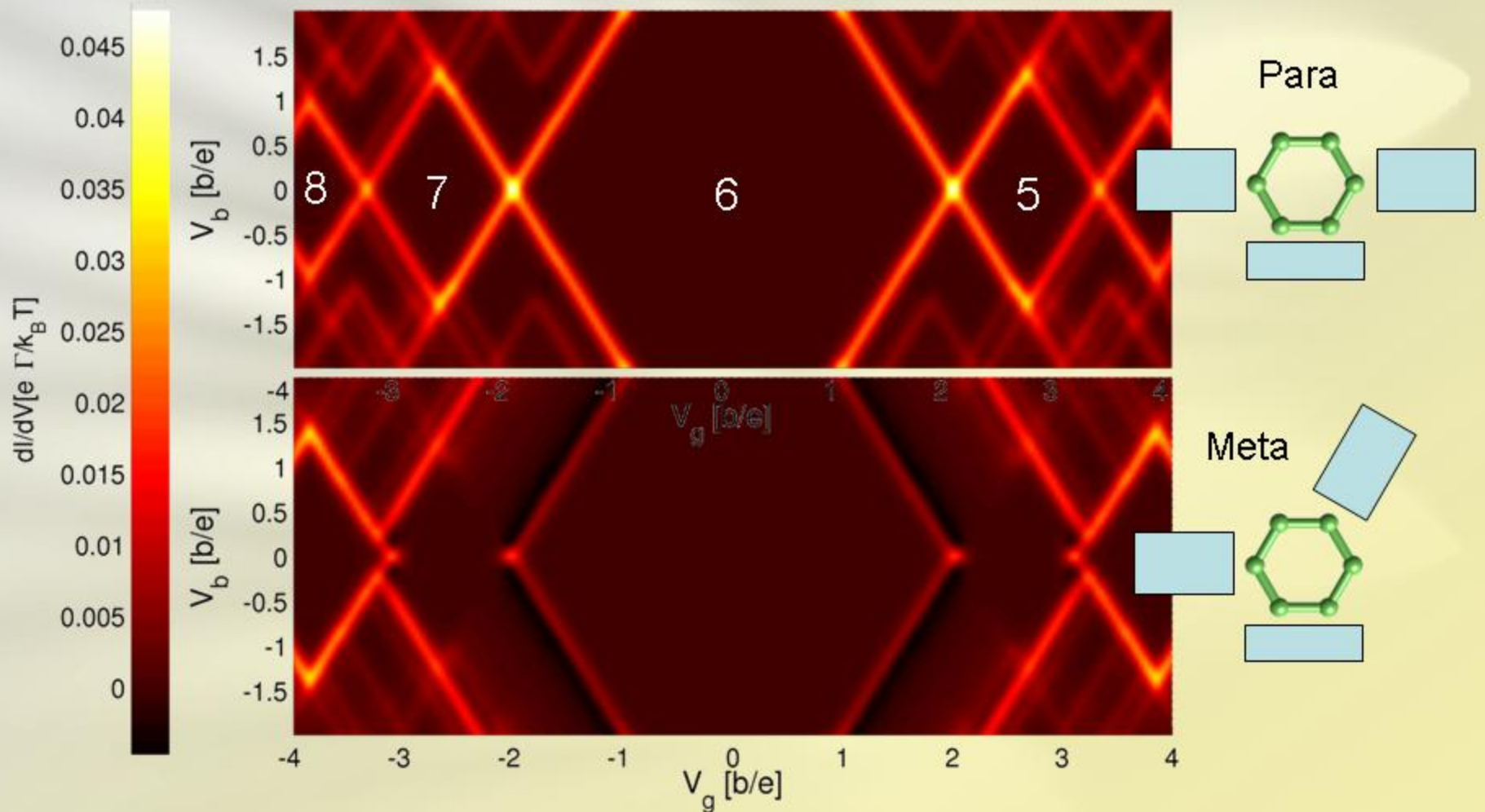
- **Current:** using the GME we find the **operator:**

$$\hat{I}_L = \Gamma_L \sum_{NE\tau} \mathcal{P}_{NE} \left[ d_{L\tau} f_L^+ (H_{\text{ben}}^0 - E) d_{L\tau}^\dagger - d_{L\tau}^\dagger f_L^- (E - H_{\text{ben}}^0) d_{L\tau} \right] \mathcal{P}_{NE}.$$

and thus calculate the **stationary current:**

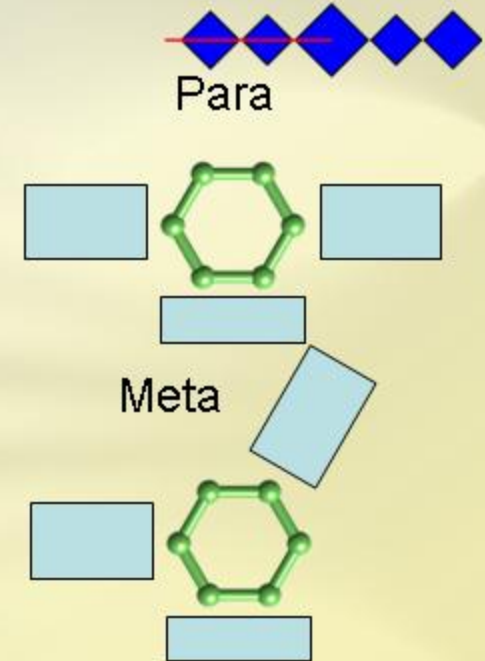
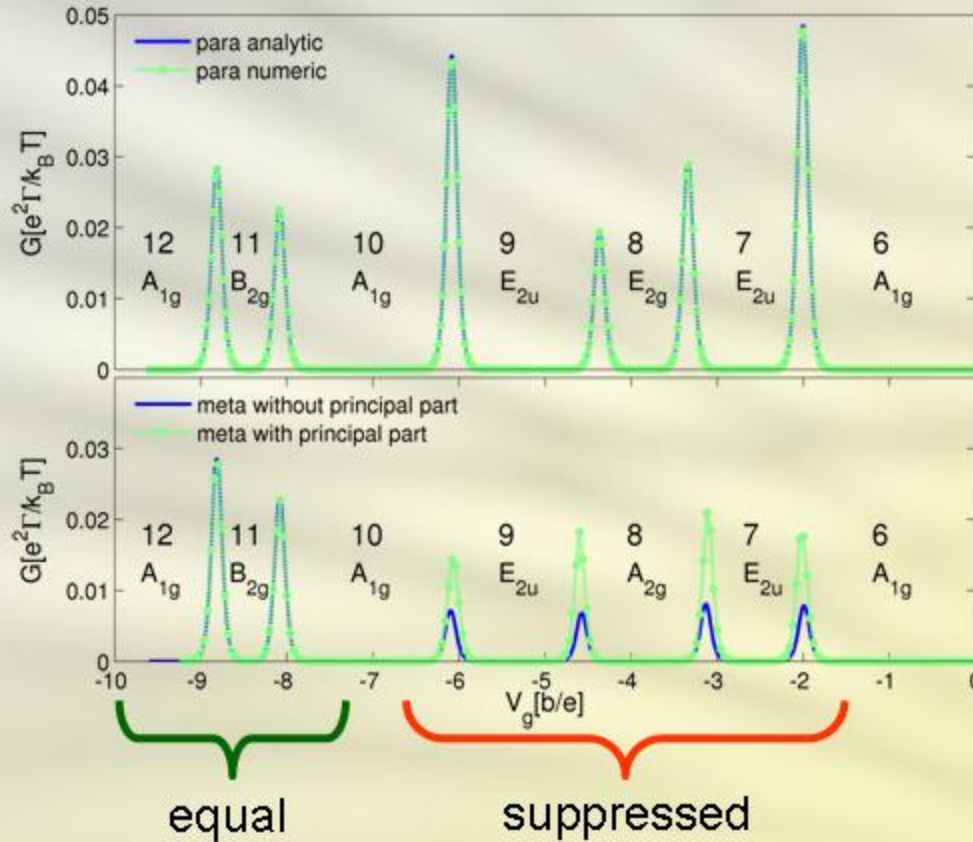
$$I_L = \text{Tr}\{\sigma_{\text{stat}} \hat{I}_L\} = -I_R$$

# Para vs. Meta



G. Begemann, D. Darau, **AD**, M. Grifoni, Phys. Rev. B **77**, 201406(R) (2008)

# Conductance suppression



**A:** non-degenerate  $\longleftrightarrow$  **B:** non-degenerate  $\Rightarrow$  Equal

**A:** non-degenerate  $\longleftrightarrow$  **E:** degenerate  $\Rightarrow$  Suppressed



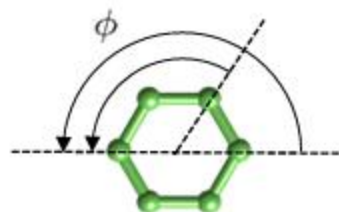
# Destructive interference

$$\Lambda = \left| \sum_{nm\tau} \langle N, n | d_{L\tau} | N+1, m \rangle \langle N+1, m | d_{R\tau}^\dagger | N, n \rangle \right|^2$$

Interference  
factor

$$\Lambda = \left| \sum_{nm\tau} |\langle N, n | d_{L\tau} | N+1, m \rangle|^2 e^{i\phi_{nm}} \right|^2$$

$$d_{R\tau}^\dagger = \mathcal{R}_\phi^\dagger d_{L\tau}^\dagger \mathcal{R}_\phi$$

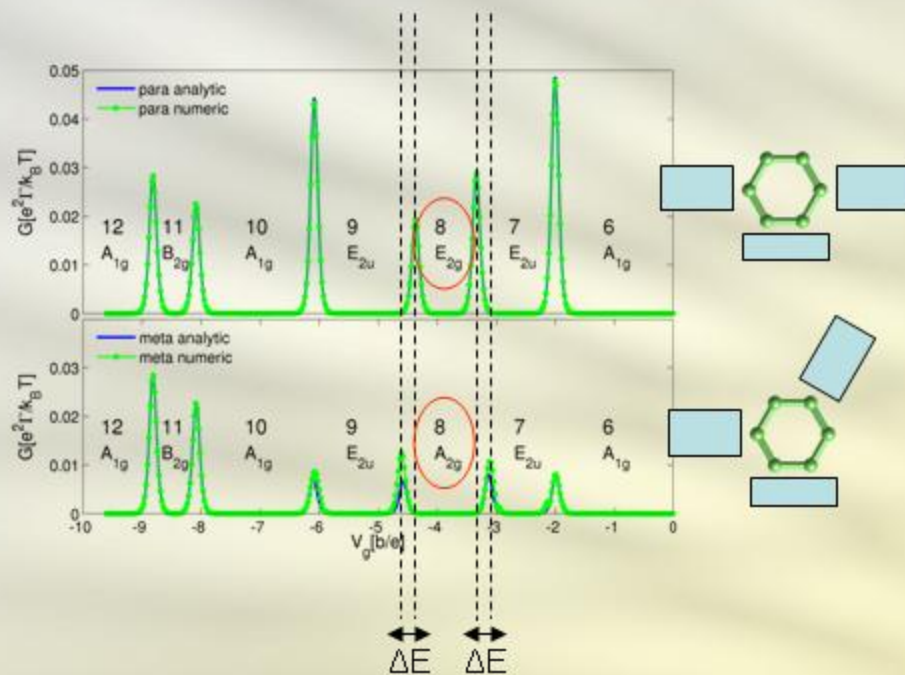


In particular for the transition **6-7** in the **meta** configuration:

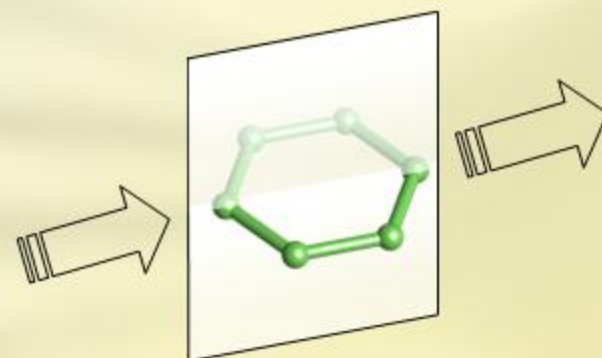
$$\Lambda = \left| |\langle 6_g | d_{L\tau} | 7_g, +2, \tau \rangle|^2 e^{+i\frac{2\pi}{3}} + |\langle 6_g | d_{L\tau} | 7_g, -2, \tau \rangle|^2 e^{-i\frac{2\pi}{3}} \right|^2$$

$$= \left| \left( \text{Green Ring } e^{+i\frac{2\pi}{3}} + \text{Red Ring } e^{-i\frac{2\pi}{3}} \right)^2 \right.$$

# The 8 electrons "anomaly"



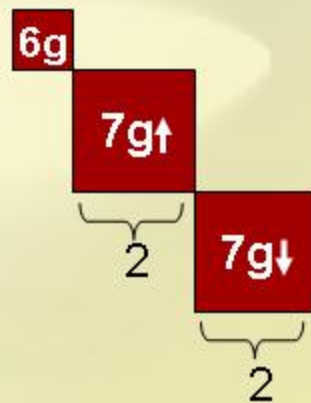
Mirror symmetry of the para-configuration



The tunnelling preserves this **mirror symmetry**: the lowest 8 electron state involved in transport is the mirror-symmetric (first excited) state with  $E_{2g}$  symmetry.

# NDC: the role of coherences

- The 7 particle ground state has spin and orbital **degeneracies**;
- **Physical basis**: the basis that diagonalizes the stationary density matrix;
- The physical basis **depends on the bias**: in whatever reference basis, **coherences** are essential for a correct description of the system;
- The **visualization tool**: **position resolved** transition probability to the physical basis:



$$P(x, y; \ell\tau) = \lim_{L \rightarrow \infty} \sum_{\sigma} \frac{1}{2L} \int_{-L/2}^{L/2} dz |\langle 7_g \ell\tau | \psi_{\sigma}^{\dagger}(\vec{r}) | 6_g \rangle|^2$$

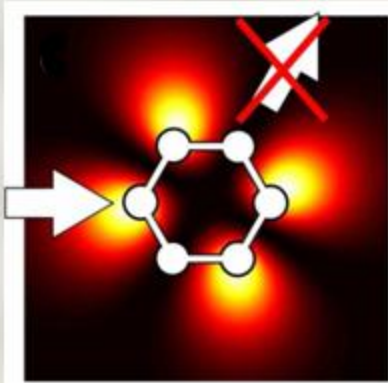
# Interference blockade

Geometry

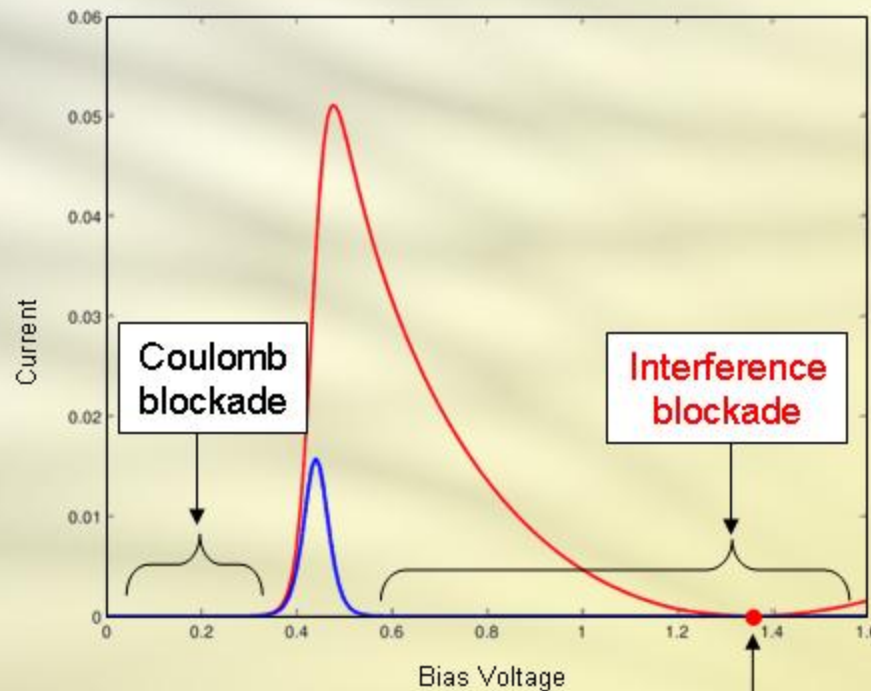
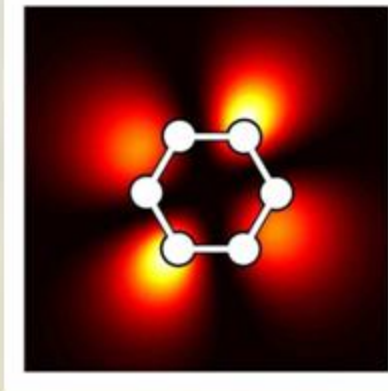
I-V for transition 6 -7

Energetics

Blocking state

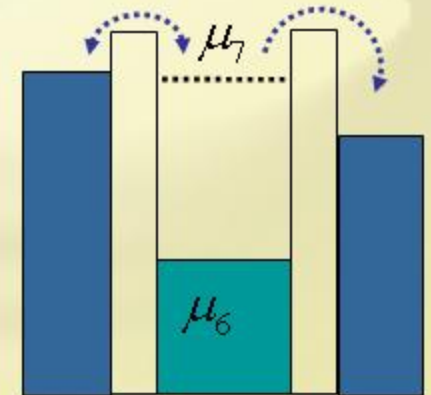


Non-blocking state

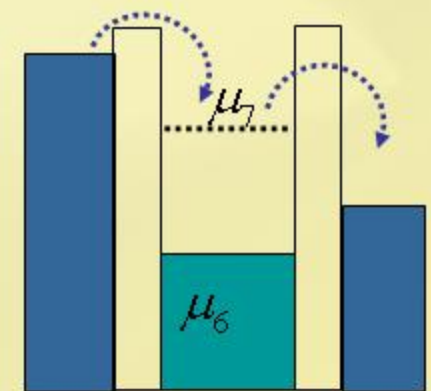


The **blocking state** is an eigenstate of the effective Hamiltonian

$$\omega_{L\sigma} = 0$$

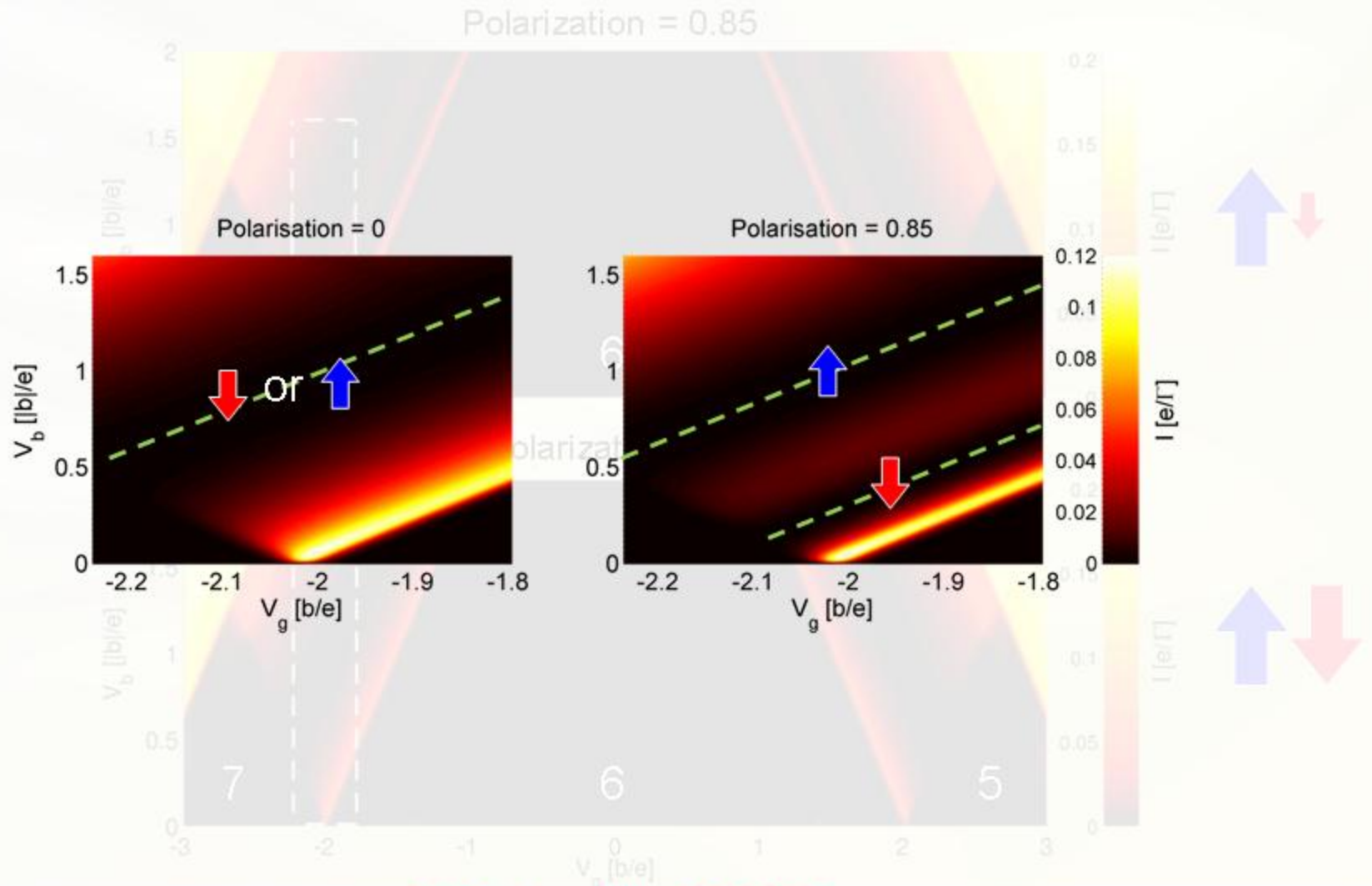


current onset

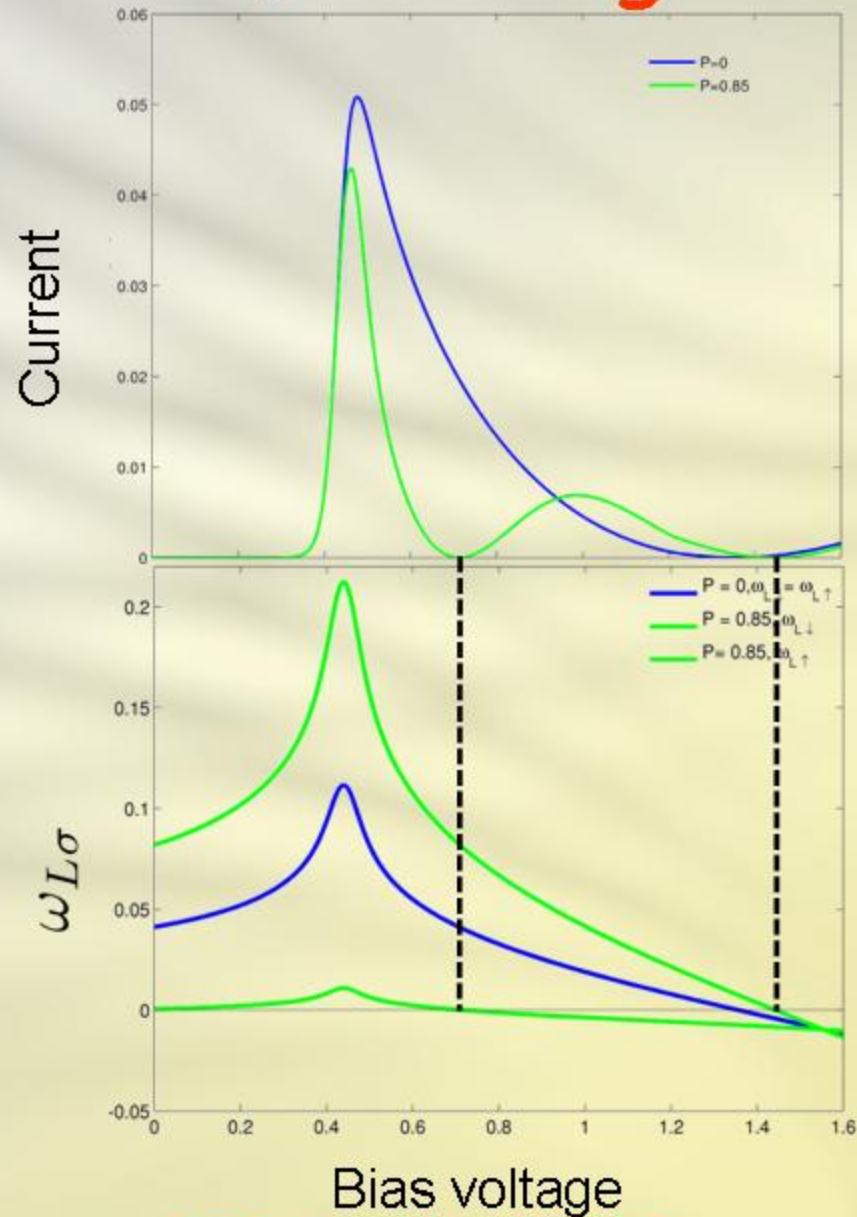


blockade

# Normal vs. ferromagnetic leads



# Normal vs ferromagnetic leads



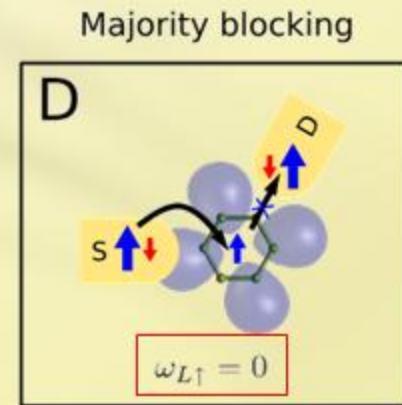
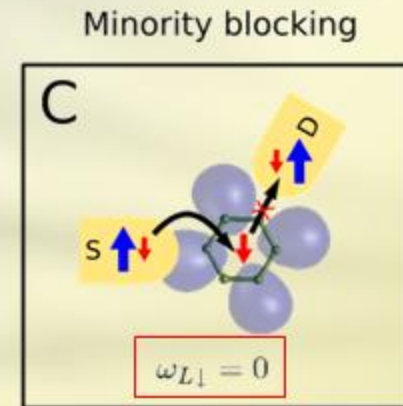
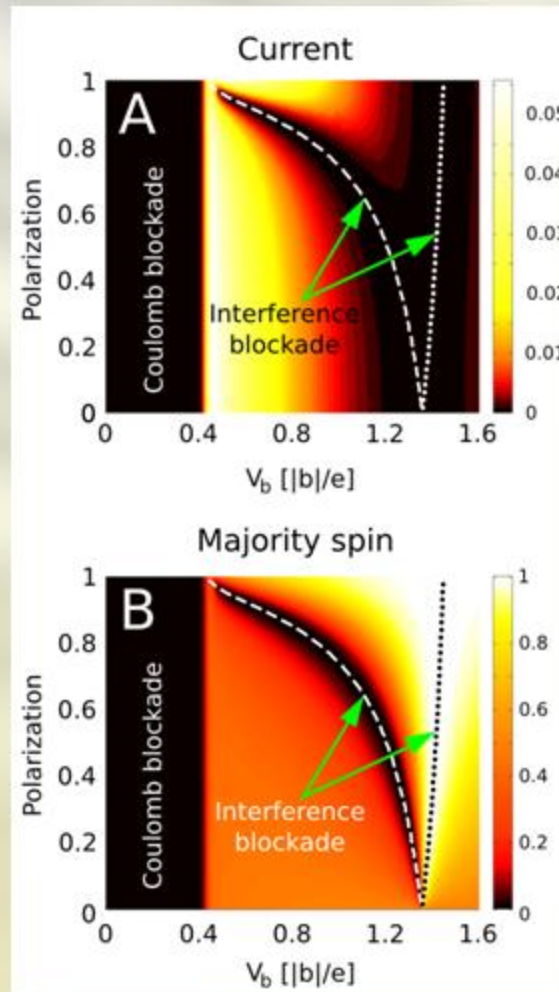
# Level renormalization in presence of polarized leads

We obtain a difference in the renormalization frequencies for the 2 spin directions linear in the **polarization of the leads**:

$$\omega_{\alpha\uparrow} - \omega_{\alpha\downarrow} = 2\bar{\Gamma}_{\alpha}^0 P_{\alpha} \frac{1}{\pi} \sum_{\{E\}} \left[ \begin{aligned} &\langle 7_g \ell \uparrow | d_{M\uparrow} | 8\{E\} \rangle \langle 8\{E\} | d_{M\uparrow}^{\dagger} | 7_g m \uparrow \rangle p_{\alpha}(E - E_{7_g}) \\ &+ \langle 7_g \ell \uparrow | d_{M\uparrow}^{\dagger} | 6\{E\} \rangle \langle 6\{E\} | d_{M\uparrow} | 7_g m \uparrow \rangle p_{\alpha}(E_{7_g} - E) \\ &- \langle 7_g \ell \uparrow | d_{M\downarrow} | 8\{E\} \rangle \langle 8\{E\} | d_{M\downarrow}^{\dagger} | 7_g m \uparrow \rangle p_{\alpha}(E - E_{7_g}) \\ &- \langle 7_g \ell \uparrow | d_{M\downarrow}^{\dagger} | 6\{E\} \rangle \langle 6\{E\} | d_{M\downarrow} | 7_g m \uparrow \rangle p_{\alpha}(E_{7_g} - E) \end{aligned} \right]$$

The splitting of the level renormalization depends crucially on the Coulomb interaction on the molecule and **vanishes in absence of exchange**.

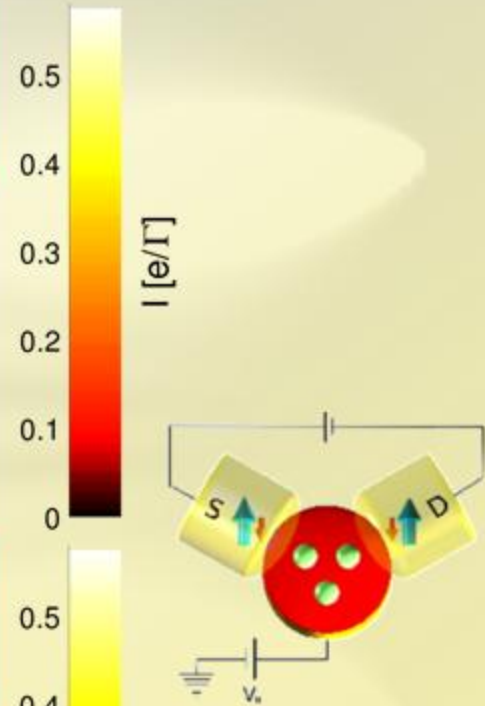
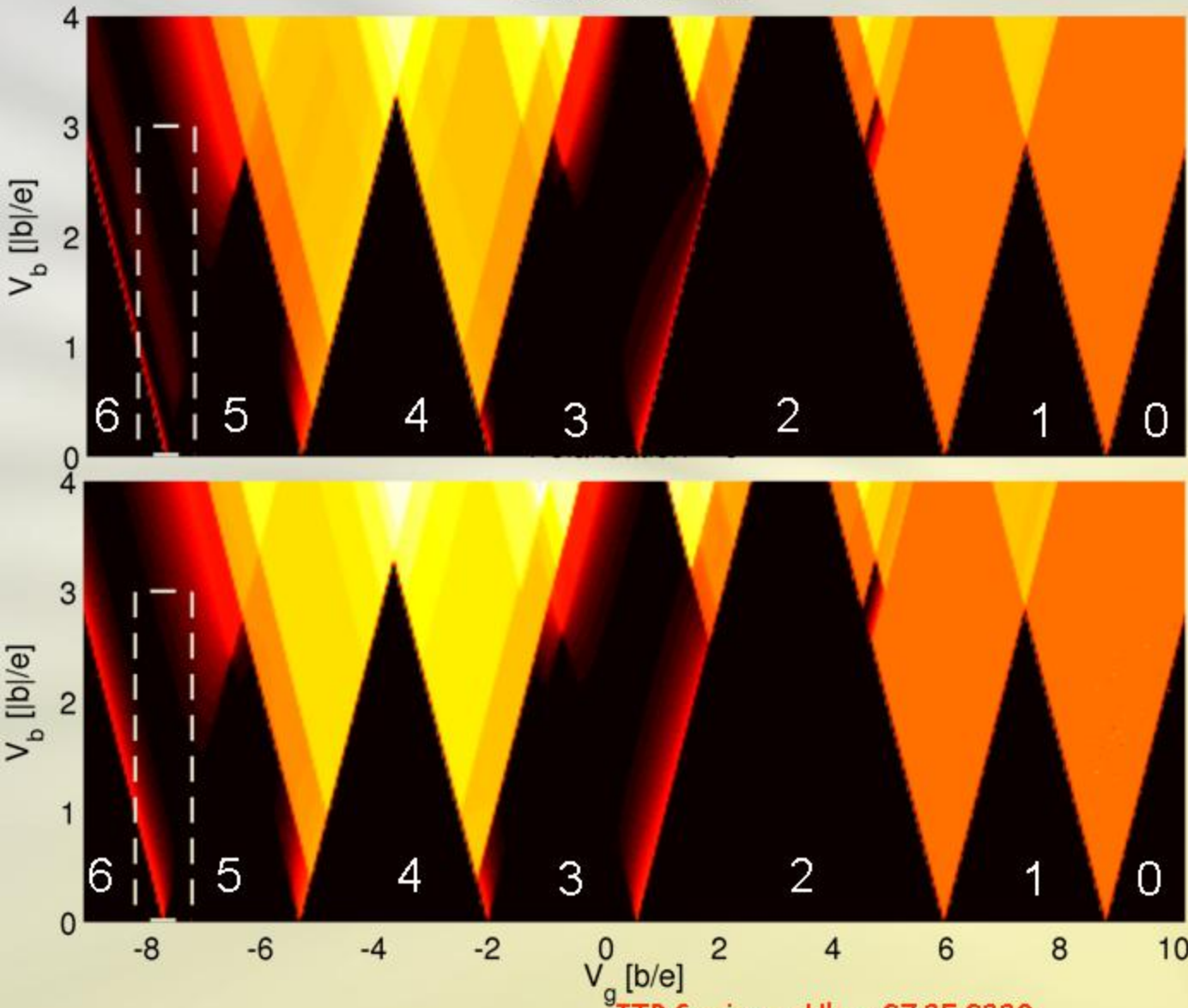
# Selective Interference Blocking





# Triple dot: Stability diagram

Polarisation = 0.7



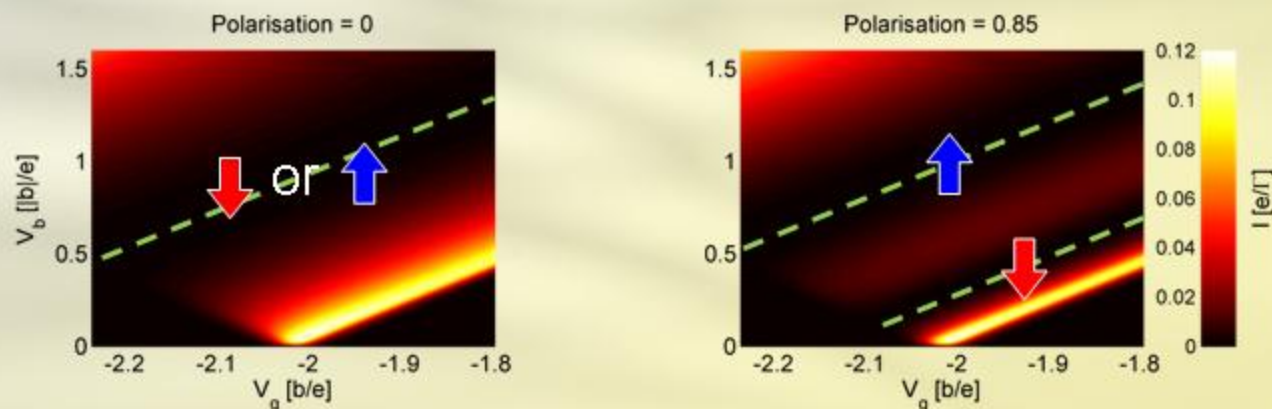
# Robustness

- We have tested the **robustness** of the effects against:
  - Residual **potential drop** on the benzene molecule (in weak coupling to the leads the potential drop is concentrated at the contacts)
  - On-site **energy renormalization** of the contact atom due to different anchor groups
  - Lifting of the electronic degeneracy due to deformation (**static Jahn-Teller effect**)
- The minimal necessary condition is **quasi-degeneracy**:

$$\delta E \ll \hbar\Gamma$$

# Conclusions

- The interplay between electron-electron **interaction** and orbital **symmetry** is important to understand transport through a benzene ISET;
- Destructive interference** between degenerate states implies current blocking at specific bias voltages.
- In presence of parallel ferromagnetic leads the **current blocking is spin-selective**. We obtain all-electrical spin control on the molecule.



- Coherences** between degenerate states are essential to capture the interference effects in a benzene ISET.
- Interference is **robust** against symmetry breaking.

# Thanks



Georg Begemann



Milena Grifoni



Dana Darau

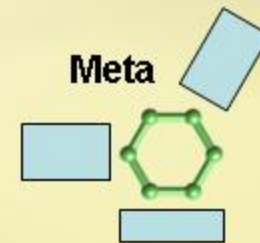
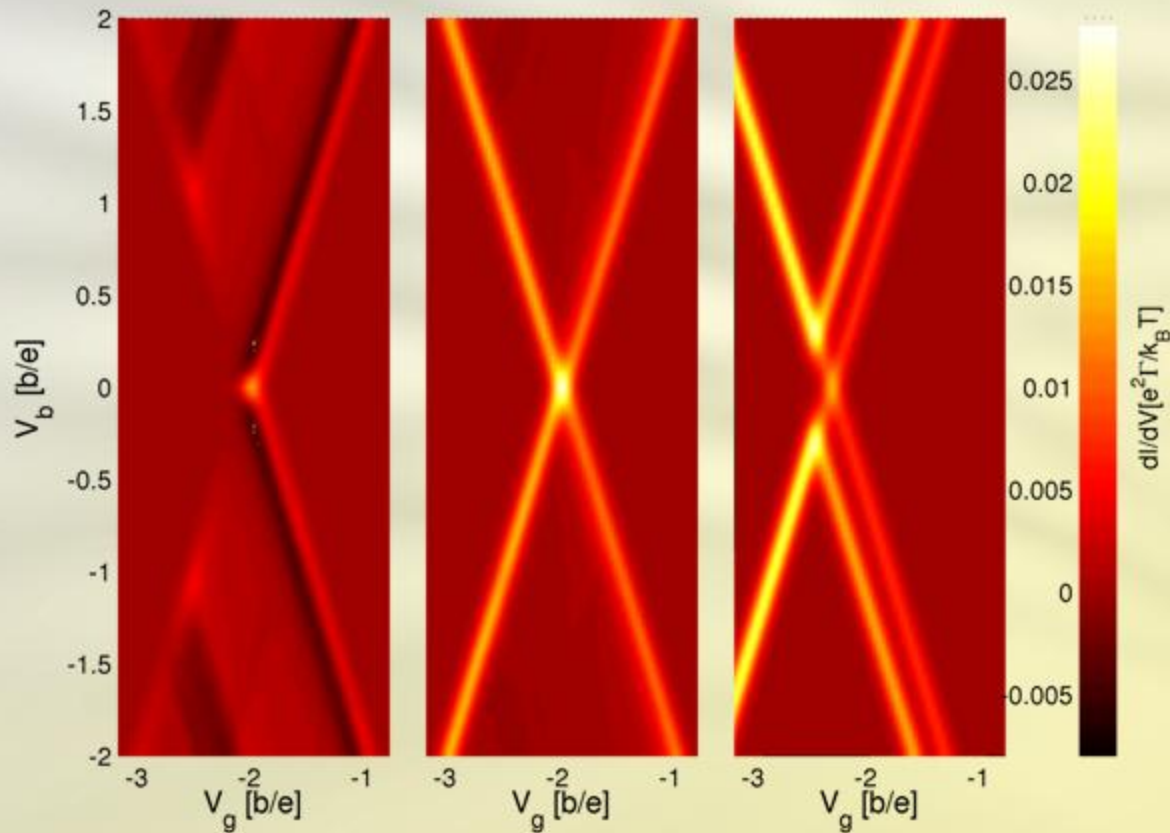
...and you for your attention!

Phys. Rev. B 77, 201406(R) (2008)

[arXiv:0904.0167](https://arxiv.org/abs/0904.0167) (Nano Lett. in press)  
[arXiv:0810.2461](https://arxiv.org/abs/0810.2461) (PRB in press)

# Contact effect

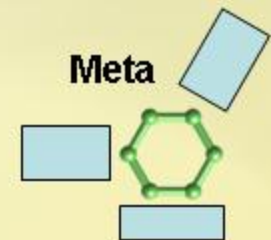
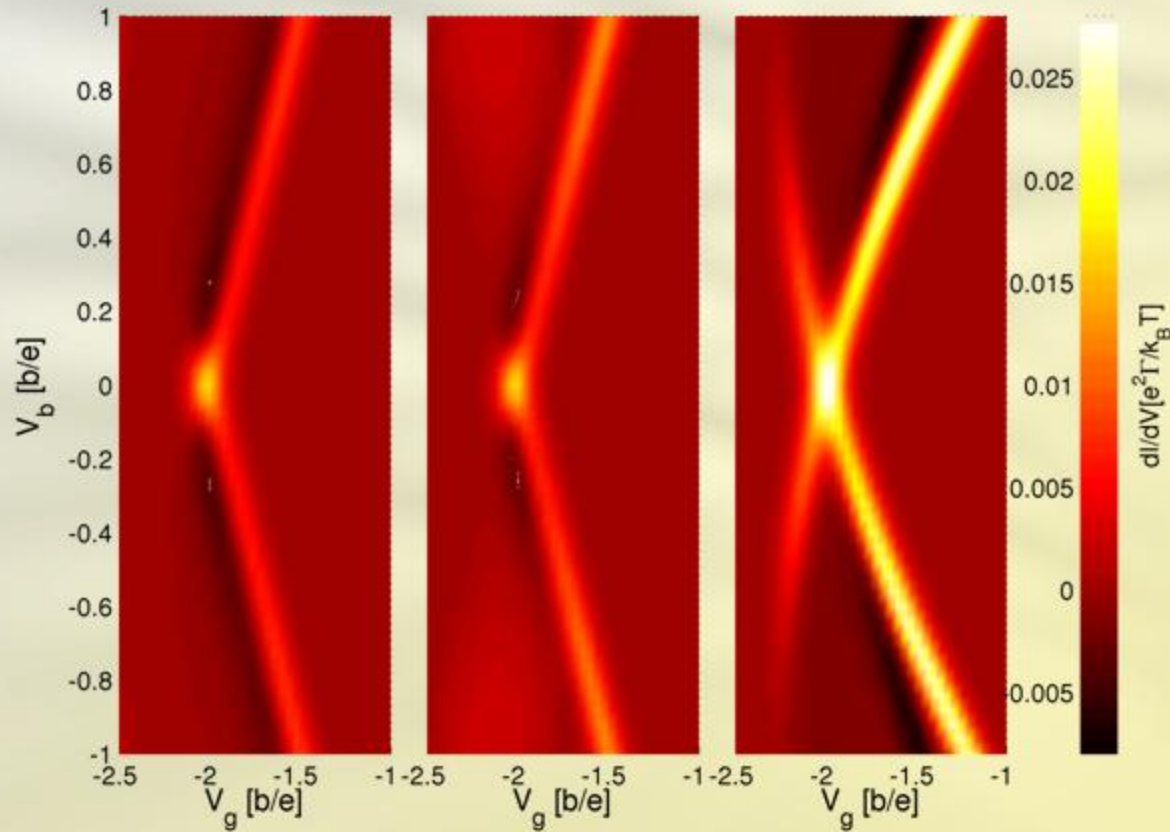
$$H'_{\text{ben}} := H_{\text{contact}} = \xi_c \sum_{\alpha\sigma} d_{\alpha\sigma}^\dagger d_{\alpha\sigma}, \quad \alpha = L, R$$



# Bias effect

$$H'_{\text{ben}} := H_{\text{bias}} = e \sum_{i\sigma} \xi_{b_i} d_{i\sigma}^\dagger d_{i\sigma}$$

$$\xi_{b_i} = \int d\mathbf{r} p_{z_i}(\mathbf{r}) V_b(\hat{\mathbf{r}}) p_{z_i}(\mathbf{r}).$$



# Bias + Contact

